

## Template functions

Function  $f$  in  $d(f, \mathbf{x})$  does not have to be defined, it can be a template function with just a name and an argument list. The argument list determines the result. For example,  $d(f(\mathbf{x}), \mathbf{x})$  evaluates to itself because  $f$  depends on  $x$ . However,  $d(f(\mathbf{x}), y)$  evaluates to zero because  $f$  does not depend on  $y$ .

Example 1.  $f(x)$  depends on  $x$ .

$d(f(\mathbf{x}), \mathbf{x})$

$d(f(x), x)$

Example 2.  $f(x)$  does not depend on  $y$ .

$d(f(\mathbf{x}), y)$

0

Example 3.  $f(x, y)$  depends on both  $x$  and  $y$ .

$d(f(\mathbf{x}, y), y)$

$d(f(x, y), y)$

Example 4.  $f()$  is a wildcard that matches any symbol.

$d(f(), t)$

$d(f(), t)$

Template functions are useful for working with differential forms. For example, show that

$$\nabla \cdot (\nabla \times \mathbf{F}) = 0$$

$\mathbf{F} = (F_x(), F_y(), F_z())$

$\text{div}(\text{curl}(\mathbf{F}))$

0