## Balmer's formula

The following table is from "Note on the spectral lines of hydrogen" by J. J. Balmer dated 1885. Numerical values are wavelengths in units of  $10^{-10}$  meter.

Investigator	$H_{\alpha}$	$H_{\beta}$	$H_{\gamma}$	$H_{\delta}$	$H_{\epsilon}$	$H_{\zeta}$	$H_{\eta}$	$H_{\vartheta}$	$H_{\iota}$
Van der Willigen	6565.6	4863.94	4342.80	4103.8	_	_	_	_	—
Angstrom	6562.10	4860.74	4340.10	4101.2	_	_	_	_	_
Mendenhall	6561.62	4860.16	_	_	_	_	_	_	_
Mascart	6560.7	4859.8	_	_	_	_	_	-	_
Ditscheiner	6559.5	4859.74	4338.60	4100.0	_	_	-	-	_
Huggins	_	_	_	_	_	3887.5	3834	3795	3767.5
Vogel	-	-	-	-	3969	3887	3834	3795	$3769^{\dagger}$

(<sup>†</sup>The value given in the paper is 6769 which is an obvious typo.)

Balmer discovered the following formula for fitting the data ( $\lambda$  is wavelength).

$$\lambda = \frac{m^2}{m^2 - 2^2} \times 3645.6 \times 10^{-10} \,\mathrm{meter}$$

Parameter m is from the following table.

Let  $\beta$  be the model coefficient for  $\lambda$ . Using linear regression and the above data we obtain

$$\beta = 3645.3 \times 10^{-10} \,\mathrm{meter}$$

The currently accepted value is

$$\beta = \frac{4}{R_H} = 3647.1 \times 10^{-10} \,\mathrm{meter}$$

where  $R_H$  is the Rydberg constant for hydrogen

$$R_H = 1.09677576 \times 10^7 \,\mathrm{meter}^{-1}$$

Balmer's coefficient is within 0.04% of the modern value.

$$100 \times \frac{4/R_H - 3.6456}{4/R_H} = 0.04$$